

K-space

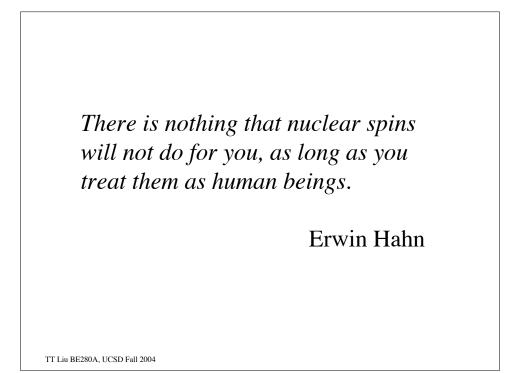
At each point in time, the received signal is the Fourier transform of the object

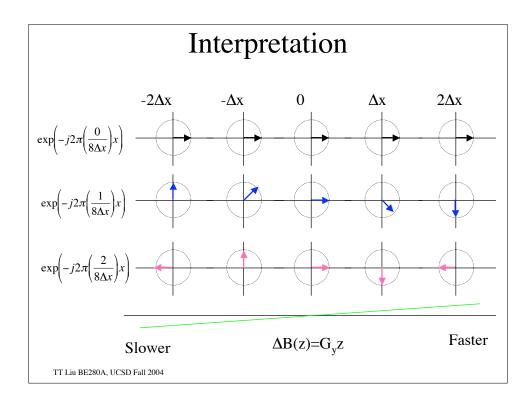
 $s(t) = M(k_x(t), k_y(t)) = F[m(x, y)]_{k_x(t), k_y(t)}$

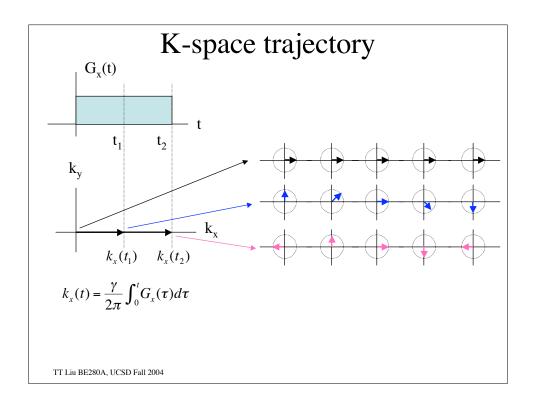
evaluated at the spatial frequencies:

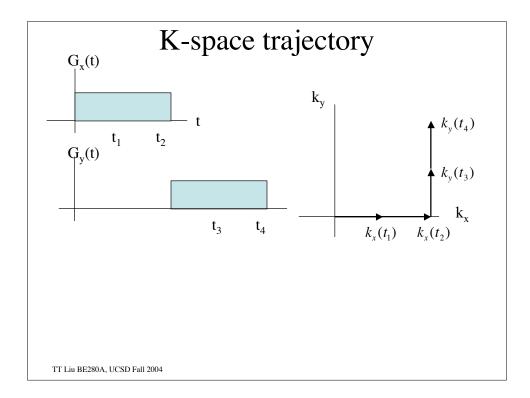
$$k_x(t) = \frac{\gamma}{2\pi} \int_0^t G_x(\tau) d\tau$$
$$k_y(t) = \frac{\gamma}{2\pi} \int_0^t G_y(\tau) d\tau$$

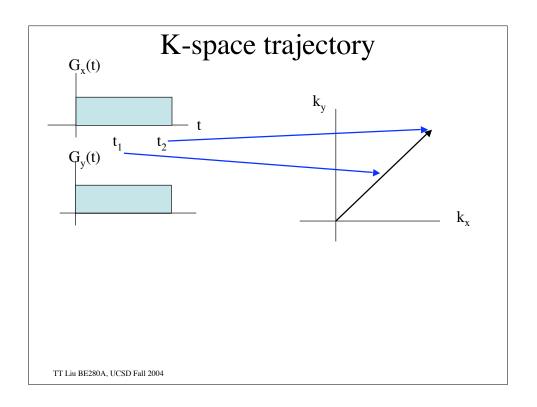
Thus, the gradients control our position in k-space. The design of an MRI pulse sequence requires us to efficiently cover enough of k-space to form our image.

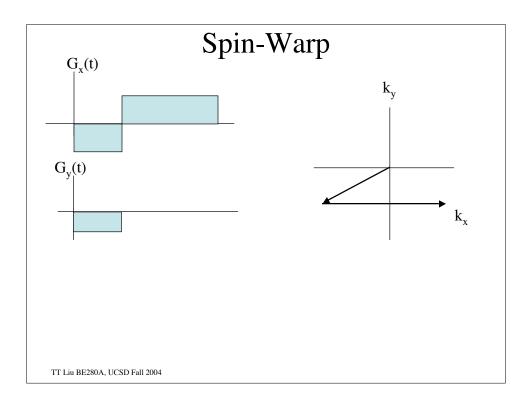


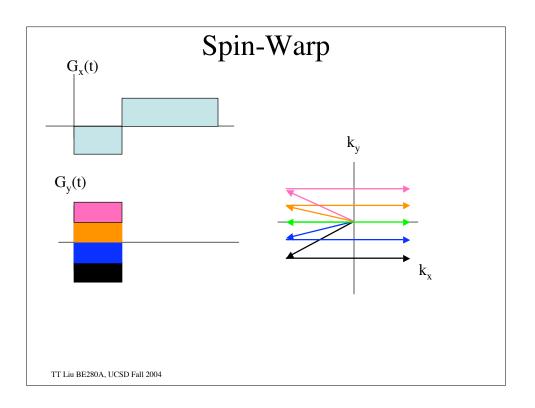


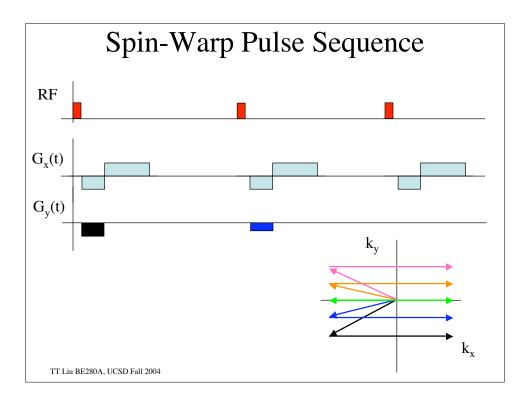


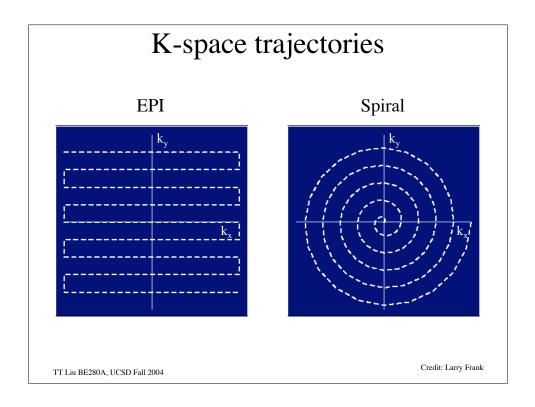


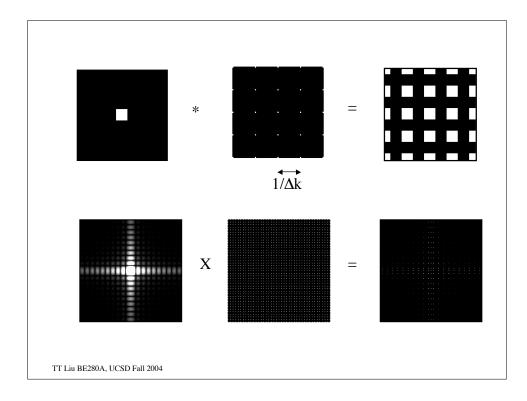


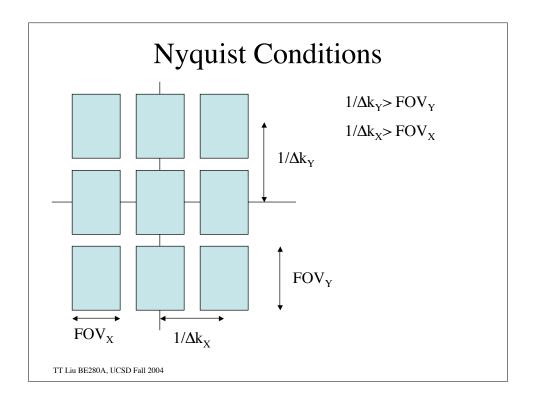


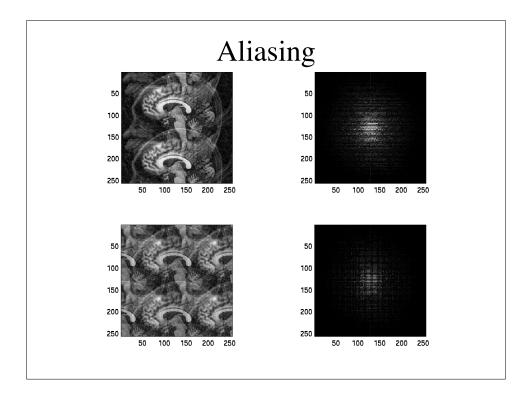


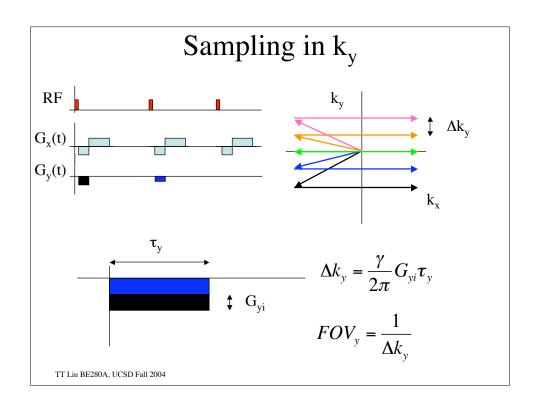


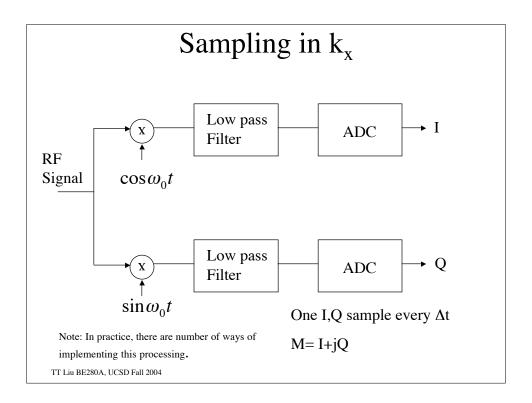


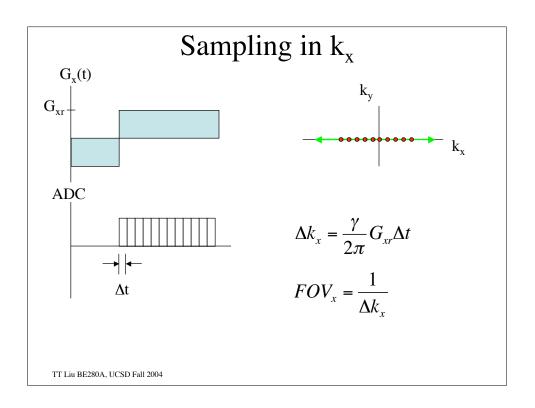


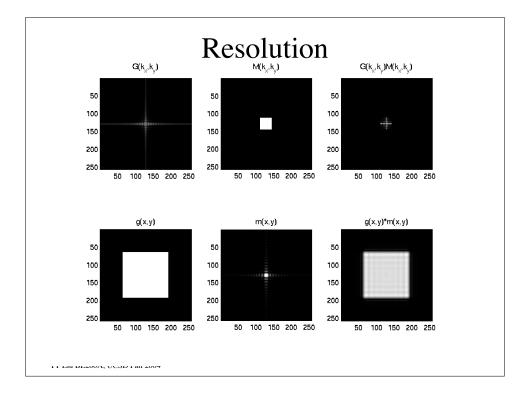


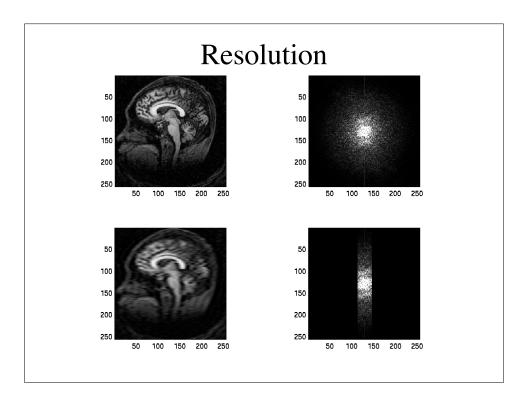


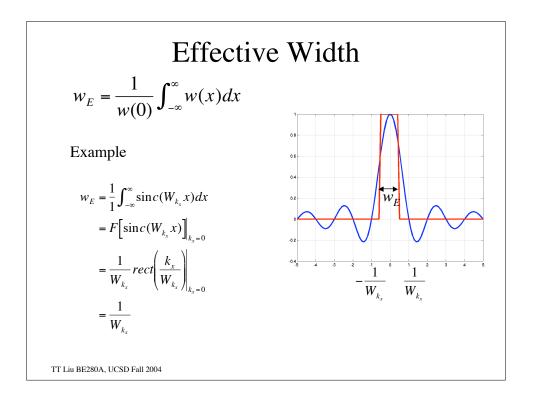


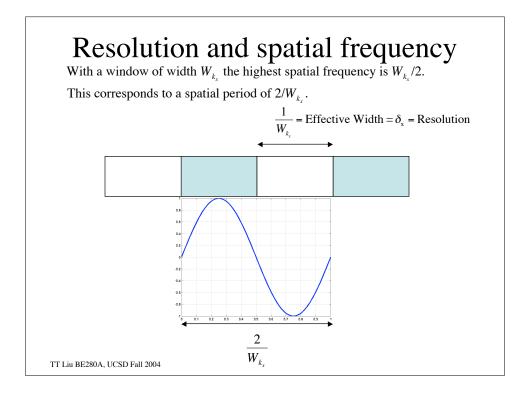


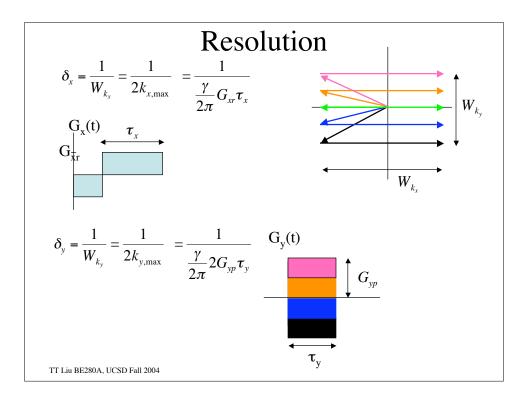


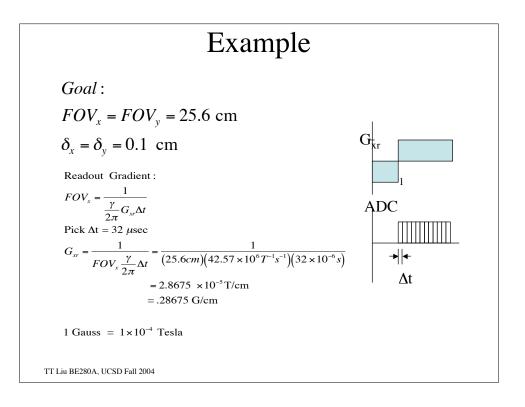


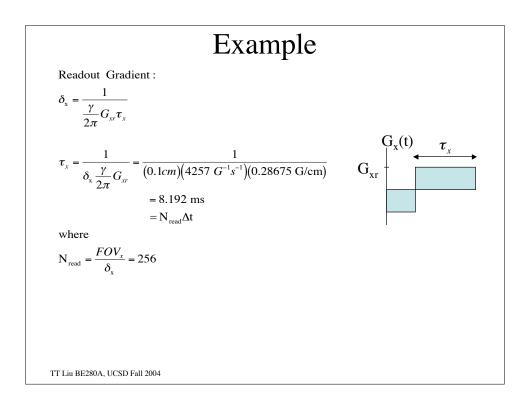


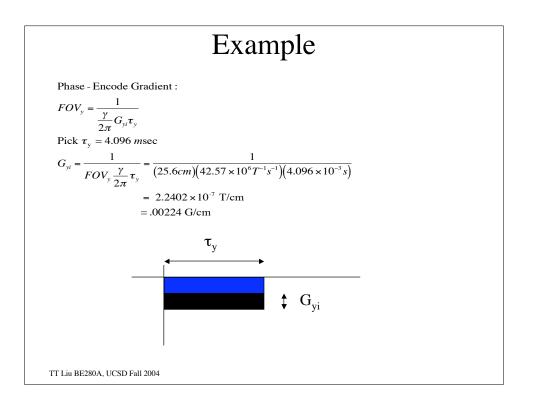


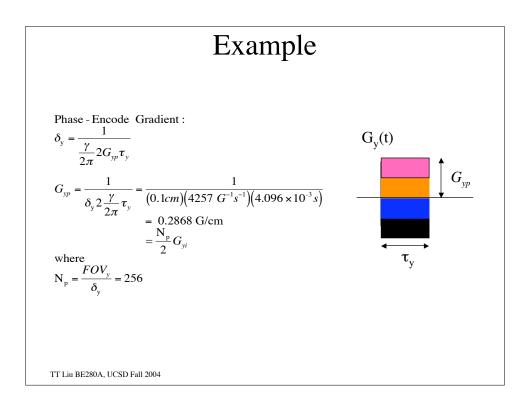


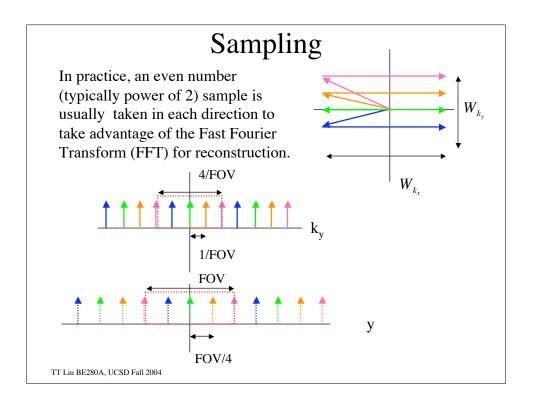


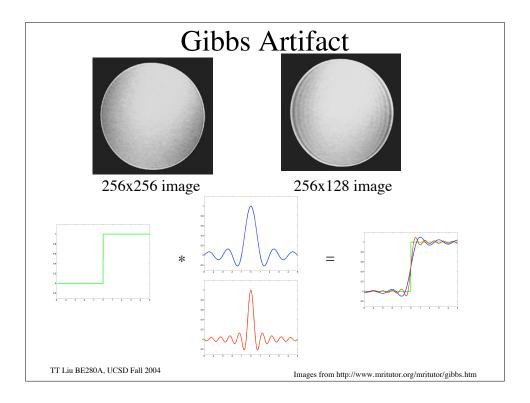


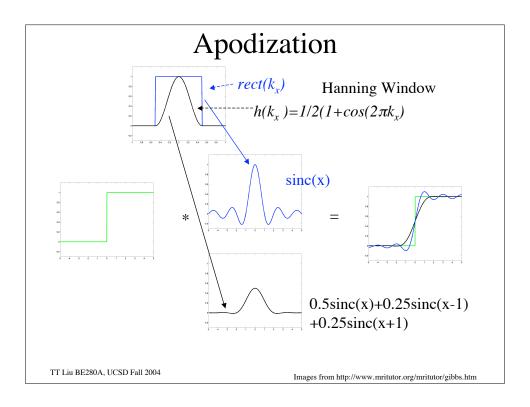


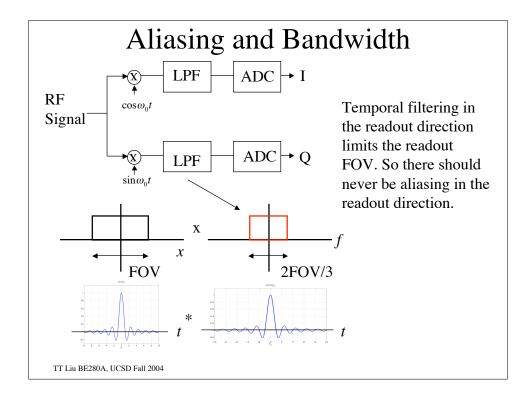


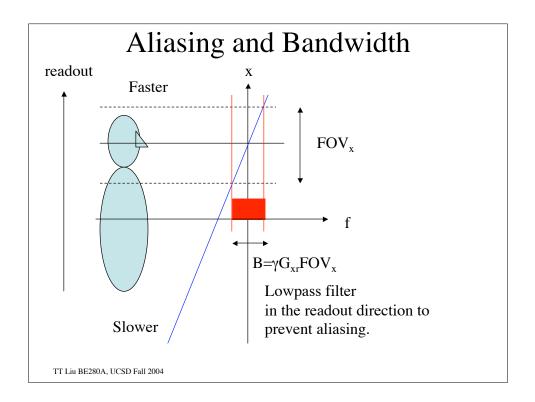


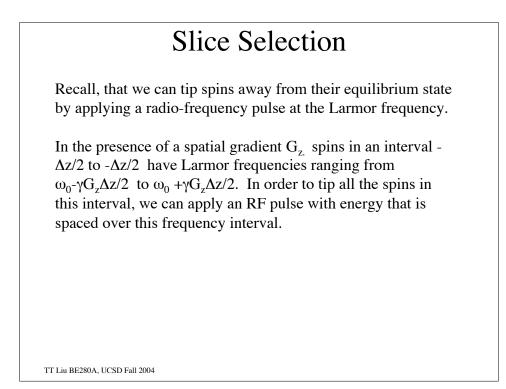


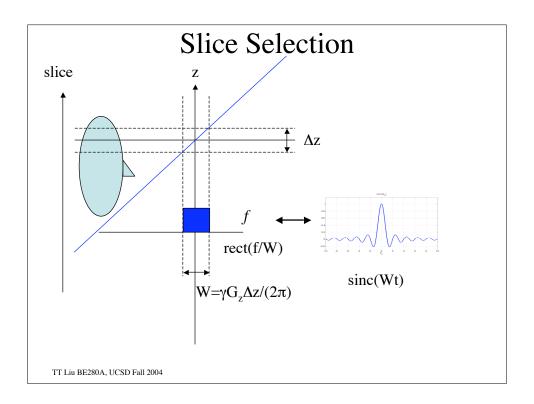


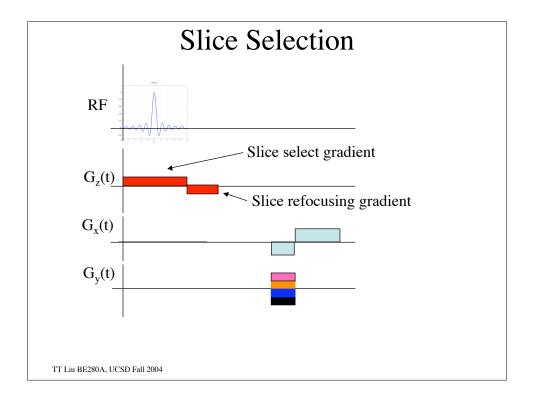


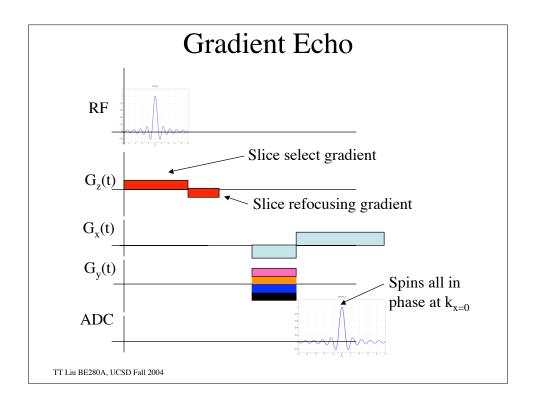












Static Inhomogeneities

In the ideal situation, the static magnetic field is totally uniform and the reconstructed object is determined solely by the applied gradient fields. In reality, the magnet is not perfect and will not be totally uniform. Part of this can be addressed by additional coils called "shim" coils, and the process of making the field more uniform is called "shimming". In the old days this was done manually, but modern magnets can do this automatically.

In addition to magnet imperfections, most biological samples are inhomogeneous and this will lead to inhomogeneity in the field. This is because, each tissue has different magnetic properties and will distort the field.

Static Inhomogeneities

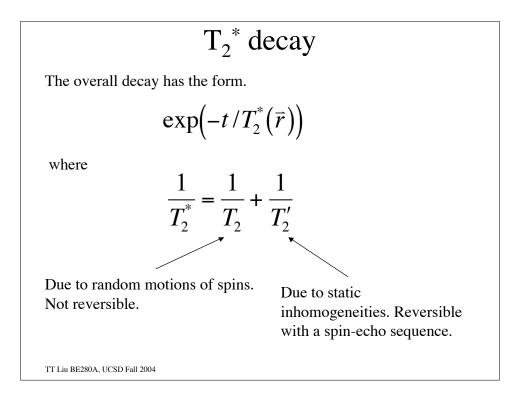
The spatial nonuniformity in the field can be modeled by adding an additional term to our signal equation.

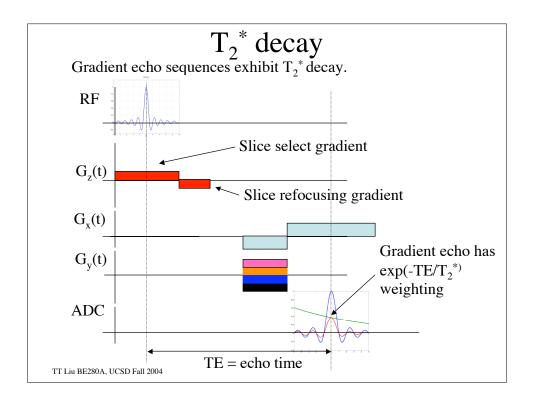
$$s_r(t) = \int_V M(\vec{r}, t) dV$$

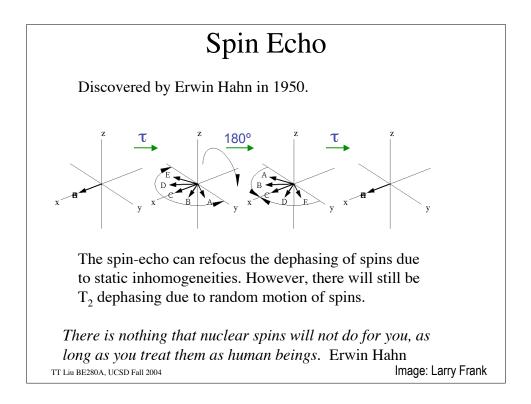
= $\int_x \int_y \int_z M(x, y, z, 0) e^{-t/T_2(\vec{r})} e^{-j\omega_0 t} e^{-j\omega_E(\vec{r})t} \exp\left(-j\gamma \int_o^t \vec{G}(\tau) \cdot \vec{r} d\tau\right) dx dy dz$

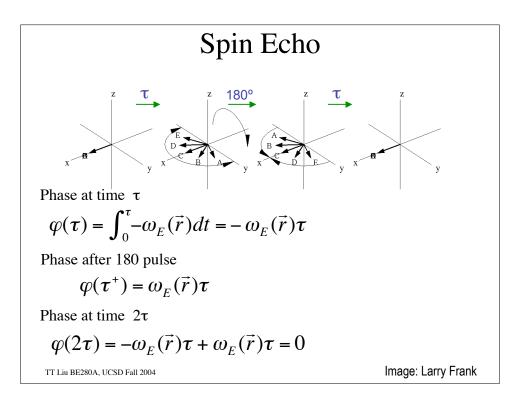
The effect of this nonuniformity is to cause the spins to dephase with time and thus for the signal to decrease more rapidly. To first order this can be modeled as an additional decay term of the form

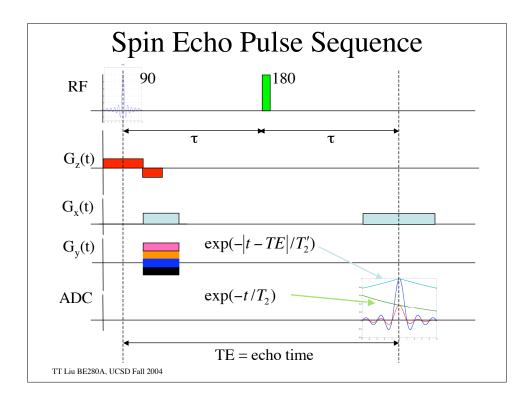
$$s_{r}(t) = \int_{x} \int_{y} \int_{z} M(x, y, z, 0) e^{-t/T_{2}(\vec{r})} e^{-t/T_{2}'(\vec{r})} e^{-j\omega_{0}t} \exp\left(-j\gamma \int_{o}^{t} \vec{G}(\tau) \cdot \vec{r} d\tau\right) dx dy dz$$

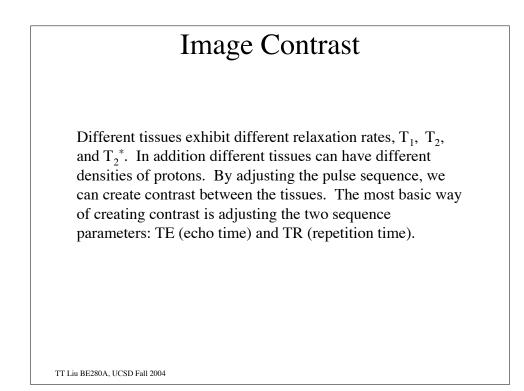


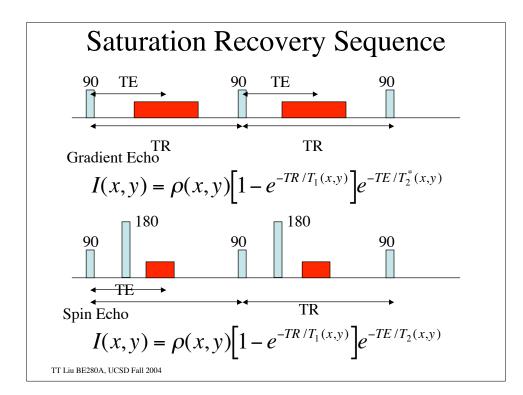












T1-Weighted Scans

Make TE very short compared to either T_2 or T_2^{*} . The resultant image has both proton and T_1 weighting.

$$I(x,y) \approx \rho(x,y) \left[1 - e^{-TR/T_1(x,y)}\right]$$

TT Liu BE280A, UCSD Fall 2004

T2-Weighted Scans

Make TR very long compared to T_1 and use a spin-echo pulse sequence. The resultant image has both proton and T_2 weighting.

$$I(x,y) \approx \rho(x,y) e^{-TE/T_2}$$

